## BRIEF INTRODUCTION TO THE STATISTICS PACKAGE R

R is a freely available language and environment for statistical computing and visualisation. It is popular for data analysis, research and teaching. Courses following on from MA10212 will use R for statistical computations.

This brief introduction is intended to teach the basic points of R: starting and quitting the package, the help facilities, doing arithmetic, command structures, functions and graphics. For those of you who already know MATLAB, there is a table for MATLAB  $\leftrightarrow$  R translation.

There are two ways to run R: the basic version of R and RStudio. The commands that you give in your code are the same in both cases. While R may be simpler to use, in RStudio it is easier to navigate directories, open and close files, etc. RStudio also has report writing features that will be used in later Statistics courses. These notes describe both R and RStudio.

#### Starting R or RStudio

If you wish to run R on your own laptop or PC, you must first download and install R. In order to use RStudio you must download and install both R and RStudio. See the final section of this document for more on installation.

On campus, you can log on to a University of Bath Public Access PC. To use a University of Bath server remotely, go to

# https://uniapps.campus.bath.ac.uk/RDWeb/Pages/en-US/Default.aspx and select the R\_RStudio icon.

In order to access R, bring up the Start menu, scroll through the list of programs until you find "R", left click on "R", then left click on "Rx64 4.0.2" (or similar). To access RStudio, bring up the Start menu, scroll through the programs until you find "RStudio", left click on "RStudio", then left click on the next "RStudio".

## Overview

On starting R or RStudio, you see the R console window. The simplest thing to do (which we shall discourage later) is to type commands in the console. Experiment by typing some commands (here > is the prompt produced by R):

> 3 + 4 > sin(pi/2) > exp( -2 ) > a <-2



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R is a command line package, rather than a menu-driven one. It usually returns the prompt >. Generally R uses brackets at the end of a name to indicate that it is a command or function (the brackets may contain arguments for the function). For example, if you want to list the objects currently stored in R, you need to type the command ls() at the > prompt, i.e.,

> ls()

If you type 1s without brackets, R prints the inner workings of the function 1s — try it and see. You can use the arrow keys to scroll around in what you have typed, so if you forget the brackets use the up arrow for a second attempt.

## Quitting R

When you want to stop R, type:

> q() (don't forget the brackets)

You should be asked if you want to save the workspace. It is usually a good idea to choose "yes" — only click on "no" if you do not want to save anything from this R session. When you say "yes", a workspace file will be created in the directory you are currently working in.

## Loading a saved workspace into R or RStudio

A workspace you have saved (from R or RStudio) is represented by an "R" icon in your directory. If you double left click on this icon, this will start an R session with the workspace loaded so, for example, any variables you defined and gave values to in your previous session will be there for you to use.

In order to use this workspace in RStudio, you need to start RStudio, navigate to the appropriate directory in the "Files" window, then click on ".RData".

## Writing commands in a script

For any substantial calculation, you should write commands in a "script". There you can build up your code and test it by running all or part of it as if you had typed the commands into the console. When you see what your code produces in the console window, you can make modifications and corrections as necessary.

You can save your script to a file and upload this again in a new R session. Once you have exactly what you want in your script, run the whole script to produce a clean, complete set of results in the console. Then, you can save these results along with any figures you have drawn to put into a report.

Below, we describe the details of the above process for R and RStudio.



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## Scripts, etc: The R version

#### Scripts

To start a new script, left click on "File" and then "New script". A window with the heading "Untitled - R editor" should appear.

You can type R commands in the script, line by line. Highlight part of the text in the script window with the left mouse button, then right click and choose "Run line or selection" (or just type Control R) to run these commands. The lines of code you have selected will run, just as if you had typed them into the R console.

You can have multiple script windows open at once. This can be useful if you want to create a set of functions in one script and write code that calls these functions in a different script.

You can save a script into your filespace. It helps if you first navigate to the appropriate directory by left clicking in the console window, left clicking on "File" and on "Change dir...", and selecting your directory in the browser. Now left click in the script window, click on "File" and on "Save as...", then type in the name you wish to give your saved script.

When you start a new R session and want to open a saved script, use "Change dir..." to navigate to the appropriate directory, click on "File" and on "Open script...", then select your script and click on "Open".

If, at any time, you wish to see which directory you are working in, the command

> getwd()

returns the name of your current working directory.

Although we have seen it is possible to save an R workspace, it is usually sufficient to save a script. Then you can start R, upload your saved script and run all the commands (e.g., by Control A, Control R) to set up the variables and functions defined in your script in the current workspace.

#### Saving the contents of the console window

Select "File" and "Save to file..." and specify a filename of the form yyy.txt. This will save the **commands and output** currently in the R console window, plus whatever appeared earlier in the session (which you can see by scrolling back up). You can use the contents of such a file in your solutions to Lab Sheets.

I have sometimes tried to save the console output and found I have created an empty file! To avoid this, do something in the console window, e.g., press return, just before saving. Before you close your R session, check that the newly created



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## Scripts, etc: The RStudio version

#### Scripts

After you have opened your RStudio session, you can move to the appropriate directory in your filespace. Click on "Session", "Set Working Directory" and "Choose Directory...", then navigate to your desired directory and click on "Open". The path to this directory and the files therein should be displayed in the "Files" window.

To start a new script, left click on the + symbol in the top left corner of RStudio, then click on "R Script". The new script will have a name "Untitled n". After you have typed some commands in this script, save it by clicking on the disk icon, typing a filename and clicking on "Save". The name of the saved file should appear in the tab at the top of the script and be added to the list in the Files window.

You can type R commands in the script, line by line. Highlight part of the text in the script window with the left mouse button, then click on the green arrow to run these commands. The lines of code you have selected will run, just as if you had typed them into the R console.

You can have multiple scripts open at once. This can be useful if you want to create a set of functions in one script and write code that calls these functions in a separate script.

When you start a new RStudio session and want to use a saved script, click on "Session", "Set Working Directory" and "Choose Directory...", to navigate to the appropriate directory. Then click on the yellow folder icon close to the top left corner of RStudio, select and open your script. Alternatively, left click on the name of the script in the Files window.

Although we have seen it is possible to save an RStudio workspace, it is usually sufficient to save a script. Then you can start RStudio, upload your saved script and run the commands to set up the variables and functions defined in your script in the current workspace.

#### Saving the contents of the console window

A simple way to save output in the Console window is to highlight the text using the left mouse button, copy this by right clicking and choosing "Copy" (or type Control C). Then you can paste this text into a file, e.g., a Word document.

This cutting and pasting may seem a bit crude for a sophisticated environment like RStudio. There are more elegant methods to use, such as RMarkdown, but



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## Getting help

Suppose we want to draw a histogram in R. There are several sources of help.

(i) The R help function

You can type

## > help(histogram)

Since histogram is not the relevant R command, this does not help much. Had we known that we needed the command hist, we would have typed

## > help(hist)

(ii) The on-line R help function

A more general approach to finding help is to use the web help facility by typing > help start()

```
> help.start()
```

If you are using R, an external browser window will open. In RStudio the browser will open in the internal "Help" window. This browser has links to lots of useful information, particularly "An introduction to R" and "Search engines & keywords": try typing *histogram* into the search engine and follow one or more of the links that appear.

(iii) Other information on the web

Type R histogram into Google, say, and follow some of the links. This route can often provide well written explanations that assume less technical knowledge of R than the output from commands such as help(hist).

## Using R as a calculator

R can be used as a calculator. Try

```
> 12 - 4
> cos( 0 )
> tan( pi/4)
> tan( pi/2)
```

```
> log(10)
```

None of the above commands stores the result in a variable. To assign values to an object, use either = or <-. To see the value of an object, type its name:

```
> temp2 <- 3**2
```

```
> temp2
```

```
> aa = temp2 + temp2
```



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#### Vector operations

Since data are often stored as vectors or matrices, R has a large number of functions to deal with these types of object. To illustrate vector arithmetic, we shall consider a Body Mass Index example from the book "Introductory Statistics with R" by P. Dalgaard.

R uses the notation c() to denote a vector, so to enter 6 weight measurements into a vector called weight, type

> weight <- c(60, 72, 57, 90, 95, 72) (the spaces are optional — but the commas are essential)

To carry out some further calculations, add

```
> height = c(1.75,1.80,1.65,1.90,1.74,1.91)
```

R applies arithmetic operations element by element, so in order to calculate Body Mass Index,  $weight/height^2$ , for these 6 individuals we can type

> bmi = weight / height  $\land$  2

```
> bmi
```

We can also perform various selection operations, for example

- > height[1] to find the height of the first person
- > height[c(3:5)] here, 3:5 is shorthand for the sequence 3,4,5.
- > length(height) to find the number of elements of height
- > sum(height) to find the sum of the heights
- > sum(height)/length(height) to find the average height
- > mean(height) a quicker way to find the average height
- > max(weight) to find the heaviest weight
- > range(bmi) to find the range of body mass indices

We can introduce logical operators and selection by logical conditions:

> bmi > 25 returns a vector of true and false values corresponding to whether the matching element of bmi is over 25 or not

- > weight[bmi<20] gives weights of those people with bmi less than 20
- > sort(bmi) sorts the values in bmi from smallest to largest
- > order(bmi) tells you the positions in which the ordered values of bmi, from smallest to largest, appear in the vector bmi

> height[order(bmi)] arranges the values in height in the order corresponding
to increasing values of bmi

A common mistake is to try to use height(1) — instead of height[1] — to



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## Graphics

Calling a plotting command in R opens a graphics window in the top right hand corner of the screen. In RStudio, the plot appears in the "Plots" window.

The command

> plot(height) will produce a plot of the 6 values of height (on the y-axis) against the order they occur (on the x-axis).

In R you can move plot windows or re-size them using the left mouse button on the window edge in the usual way.

In RStudio you can change the size of the Plots window and, hence, change the aspect ratio of a plot. Clicking on the arrows at the top of the Plots window will move through the current set of plots.

It is worth discovering some of the other arguments for the function plot():

```
> help(plot)
```

```
> plot(height,type="l",xlab="Order",ylab="Height",main="My plot")
To plot one object against another, give two arguments:
```

> plot(height,weight,xlab="Height",ylab="Weight",main="H-W plot")

Note which variable is plotted on the x-axis and which on the y-axis.

In R you can save a graph to a file by right clicking on the graphics window. Then, choosing "Save as metafile" will create a file with ending .emf in the directory that you specify, while "Save as postscript" will create a file with ending .eps. To view the figure later, left click on the icon for the .ems file or the .eps file and you should be able to see the content of your file using Paint or GSview, respectively.

In RStudio, you can click on "Export" and "Save as Image", then choose from a selection image formats.

In R, by default, each graphics command overwrites what is in the current graphics window. To avoid this, you can create a new window by typing

> windows()

— although you may have to move the new window to see the old one underneath!

Another useful option in both R and RStudio is to set the parameter mfrow() in order to put multiple plots on one page. Once you have set mfrow() using the par command, plots will continue to be placed in the specified format.

> par( mfrow=c(2,2) ) produces 2 rows each of 2 images

> par( mfrow=c(2 1) ) produces 2 rows each of 1 image



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## Writing a plot directly to a file

Another option is to type commands to write a plot directly to a file. Various file types are possible. Suppose, for example, you wish to save a plot of weight against height to a .png file called plot1.png. This can be achieved by typing

```
> png(filename="plot1.png")
> plot(height,weight,xlab="Height",ylab="Weight",main="H-W plot")
> dev.off()
```

In the above sequence, the first command sets up the file plot1.png as the destination for the graphic. The second command creates the plot — which should look just the same as the one previously produced on the screen. The third command ends this process, so further graphics will appear in a graphics window on the screen in the usual way.

When creating a plot this way, the file takes over the role of the window labelled "R Graphics: Device". Thus, it can contain just one plot, or an array of plots if the mfrow() command is used.

I have had problems viewing .eps files or importing them to Word documents. While an .ems file works better, this tends to contain a small graphic and a lot of empty space that can be hard to remove. Using a .png file appears to be a safe option with robust functionality.

## Combining material in your coursework solutions

For your coursework, you will combine the transcript of your R session and the resulting graphics output into a Word document. To do this, open a Word document, then cut and paste content from the .txt file containing your R session (see "Saving the contents of the console window"). You can insert the .emf, .eps or .png files for graphics showing histograms, plots, etc. To do this in Word, choose "insert", then "picture", then navigate to the .emf, .eps or .png file and load this.

Another option is to copy the graphic directly from the R graphics window then and paste this item into your Word document. In R, you can copy the graphic by right clicking and choosing "Copy as bitmap". In RStudio, click on "Export" and "Copy to Clipboard...".

Place each graphic after the R commands that produced it. Be sure to comment on what R has produced to answer the specific questions asked in the Lab Sheet. Writing these answers in colour will help highlight them for the marker.

For a really good piece of coursework, tidy up the output: remove the first



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#### Flow control

A strength of R is that you can write your own functions. Before considering an example, we need to know the flow control arguments that are available. These are the equivalent of the *for loops*, *while loops* and *if-else statements* in MATLAB: there is a translation guide at the end of this handout.

It is good to try out some of the following examples. However, it is not possible to correct errors after typing a number of lines in the console window. So, before trying examples, you may find it helpful to read the later section on **Scripts**.

The for loop:

Suppose we want to calculate  $\sum_{i=1}^{100} i^2$ . One way to do this in R is to use a for loop, putting the result in the variable sum100:

```
> sum100 <- 0
> for ( i in 1:100 )
+ {
+ sum100 <- sum100 + i**2
+ }
> sum100
```

This code sets sum100 to zero, then carries out a loop for i in  $\{1, \ldots, 100\}$ . The curly brackets  $\{ \}$  contain the commands to be carried out for each value of i. Note the R prompt changes from > to + when the current command has not yet finished (in this case, the for loop must be terminated by a final "}").

In step i, sum100 is incremented by i\*\*2, and the loop continues to the next value of i. At the end the value of sum100 is printed.

The while loop:

We can use a while loop to find the smallest **n** for which  $\sum_{i=1}^{n} i^2 > 100$ .

This code initialises the variables n to 0 and sum100 to 0 Then while the



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The if construction:

The general form of this construction is

```
> if (test condition)
+ {
+ some commands
+ }
```

If the test condition is TRUE, the commands are executed. If it is FALSE, they are ignored.

Examples of test conditions are x > y,  $x \le y$ , a==b and s != t. The last two test whether a is equal to b and whether s is NOT equal to t

The if, else construction:

The general form of this construction is

```
> if ( test condition1 )
+
   ł
    some commands1
+
+
   } else if (test condition2 )
+
+
    some commands2
   } else
+
+
+
    some commands3
+
   }
```

This structure checks to see if test condition1 is TRUE and, if so, executes some commands1. If the first condition is FALSE, it continues on to the other sections: then if test condition2 is TRUE, it executes some commands2, but if test condition2 is FALSE it executes some commands3.

You can insert more cases of else if. Alternatively, the else if part can be omitted altogether, giving a simple if command.

It is important that else if (test condition2) and else are on the same line as the preceding }. If the } were on a line by itself, this would finish the if statement, thus R executes the completed command, returning the > prompt, and the following else or else it command causes an error message.

We illustrate if and else structures in the next section, Writing R functions.



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## Writing R functions

Suppose you want to repeat a set of commands, possibly using different parameter values. Rather than type all the code each time, you can define a function to carry out the calculations, passing parameter values to the function as arguments.

We illustrate this idea with a simple function that generates and displays binomial data. Type the following commands

```
> show.binomial = function(size,n,p)
+ {
+ sample = rbinom(size,n,p)
+ # Draw a histogram of the data in sample --- this is a comment
+ hist(sample)
+ }
```

You have just defined a function called **show.binomial** which takes three parameter values. Implement the function by the command

```
> show.binomial(100,20,0.5)
```

In response, R generates a sample of 100 independent Binomial(20, 0.5) random variables (RVs) using the built in function rbinom() and draws a histogram of the 100 values. Repeat the command and experiment with other parameter values.

The following, more substantial function can be used to demonstrate that the sum of two independent binomial RVs with the same probability **p** is also binomial.

```
add.binom = function(nreps,n1,n2,p)
 ł
  sample1 <- rbinom(nreps,n1,p)</pre>
  sample2 <- rbinom(nreps,n2,p)</pre>
  sample3 <- sample1 + sample2</pre>
  par(mfrow = c(3,1))
  if (nreps > 50)
  ł
    hist(sample1, xlim=c(0,n1))
    hist(sample2, xlim=c(0,n2))
    hist(sample3, xlim=c(0,n1+n2))
  }
   else
    stripchart(sample1, method="stack", xlim=c(0,n1),
    ylim=c(0,nreps/2))
    stripchart(sample2, method="stack", xlim=c(0,n2),
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```

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#### Writing a function in a script

It is helpful to write a new function outside the R console as it is easier to make modifications and corrections. Make sure you have a script open in which to put functions. Rather than type in all the commands for the function add.binom yourself, go to the course Moodle page, click on the link to "Script for add.binom and add.binom2" under **R sessions and R code**, then cut and paste the text into your script.

Highlight and run all of the text for the function add.binom. The effect is just as if you had typed all this text into the R console. So, you have created the function add.binom. Implement it with some parameter values, e.g.,

> add.binom(100,20,20,0.4)

You should get an error message! In fact, there are two errors in the script from the Moodle page but only one will have caused a problem this time. When you have identified the error, edit the text in the Script window, run these commands again to re-define the function add.binom, and repeat the add.binom command.

The above function generates a vector of **nreps** samples from a Binomial(n1, p) distribution and another vector of **nreps** samples from a Binomial(n2, p) distribution. The vectors are added element-wise to give **nreps** realisations of a Binomial(n1+n2, p) RV. The function plots the two sets of random samples, together with their sum. If the sample size **nreps** is large, the plots are histograms, otherwise, dotplots are used. You can use the help facility to see what the arguments to these functions mean.

It is often desirable that a function generates output to be used later. We do this by stating the variable that contains the output (i.e., the name of the variable within the function) just before closing the function. Try reading in the following function add.binom2 from "Script for add.binom and add.binom2".

```
add.binom2 = function(nreps,n1,n2,p)
{
  sample1 <- rbinom(nreps,n1,p)
  sample2 <- rbinom(nreps,n2,p)
  sample3 <- sample1 + sample2
  par(mfrow = c(3,1))
  if (nreps > 50)
  {
    hist(sample1, xlim=c(0,n1))
    hist(sample2, xlim=c(0,n2))
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```

```
stripchart(sample2, method="stack", xlim=c(0,n2),
   ylim=c(0,nreps/2))
   stripchart(sample3, method="stack", xlim=c(0,n1+n2),
   ylim=c(0,nreps/2))
   }
   outvar=sum(sample1)
   outvar # This is the variable the function returns as output
   }
Then type
add.binom2(100,10,10,0.2)
and also try
```

```
ww=add.binom2(100,10,10,0.2)
```

followed by

ww

## Tidying up

You will not necessarily want to save all the objects you create during an R session. Use rm() to remove them.

> rm(height, weight, bmi)

Also, if you have finished writing a script and want to check that it does what it is meant to do, it is good to run functions and commands in a clean workspace. That way, you can be confident that the variables are being defined as intended by commands in your script and you are not just using variables that happen to exist already in your R workspace.

You can empty your workspace with the command

> rm(list=ls())

— but it goes without saying that you should use this command carefully.

## Installing R and RStudio on your own computer.

See http://www.r-project.org, if you wish to install R on your own computer (free of charge). On a UNIX or MAC platform, the software has a somewhat different appearance from that seen under Windows but its functionality will be as described here.

If you wish to run R through RStudio first install R, then download and install RStudio from https://nstudio.com/nmeduate/nstudio/download/. Note that



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## $\mathbf{MATLAB} \leftrightarrow \mathbf{R} \ \mathbf{translator}$

| COMMAND                 | MATLAB                     | R                                   |
|-------------------------|----------------------------|-------------------------------------|
| Prompt                  | >>                         | > (or + within loops)               |
| Variable assignments    | =                          | <- or =                             |
| View current variables  | who                        | ls()                                |
| Help commands           | help topic                 | help(topic)                         |
| Vectors                 | y = [0, 1, 2, 3, 4, 5]     | y <- c(0:5) or                      |
|                         |                            | y = c(0,1,2,3,4,5)                  |
| Selection from a vector | y(1:5)                     | y[1:5]                              |
| For loops               | <pre>for index = 1:n</pre> | for ( index in 1:n )                |
|                         | statements                 | {                                   |
|                         | end                        | statements                          |
|                         |                            | }                                   |
| While loops             | while ( condition )        | while ( condition )                 |
|                         | statements                 | {                                   |
|                         | end                        | statements                          |
|                         |                            | }                                   |
| If statements           | if ( condition1 )          | if ( condition1 )                   |
|                         | statementsA                | {                                   |
|                         | elseif ( condition2 )      | statementsA                         |
|                         | statementsB                | <pre>} else if ( condition2 )</pre> |
|                         | else                       |                                     |
|                         | statementsC                | statementsB                         |
|                         | end                        | } else                              |
|                         |                            |                                     |
|                         |                            | statementsC                         |
|                         |                            | }                                   |
| Remove variables        | clear                      | rm()                                |



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